

Books on Operator Algebras and prerequisites

26.1.2009

1 General Topology

- Chapter 1 of G. Bredon: *Topology and Geometry*. Springer GTM. (Very nice, contains most of general topology one ever needs.)
- Chapter 1 of G. Pedersen: *Analysis Now*. Springer GTM. (Complements previous reference.)
- V. Runde: *A taste of topology*. Springer Universitext. (Nice and readable textbook.)
- R. Engelking: *General topology*. Heldermann Verlag. (Very comprehensive, very useful for reference.)

2 Functional analysis

- G. Pedersen: *Analysis Now*. Springer GTM. (Beautiful, highly recommended.)
- J. B. Conway: *A course in functional analysis*. Springer GTM. (More comprehensive than Pedersen.)
- W. Rudin: *Functional analysis*. (Abstract approach: From the general to the particular.)
- M. Reed and B. Simon: *Functional analysis*. [Vol. 1 of series on mathematical physics.] (Nice, somewhat eclectic.)
- P. Lax: *Functional analysis*. (Quite different from preceding references. Many applications to classical analysis.)

3 Operator algebras

3.1 Overviews

- Chapter V of A. Connes: *Noncommutative Geometry*. Ca. 90 p. (Very inspiring.)
- Chapter 2 of O. Bratteli and D. Robinson: *Operator algebras and quantum statistical mechanics*. Vol. 1. Ca. 150 pages. Springer. (Brief crash course for aspiring mathematical physicists.)
- R. Bhat (ed.): *Lectures on operator theory*. AMS. (Mixed quality, but nice for a first impression.)

- B. Blackadar: Operator algebras. Theory of C^* -algebras and von Neumann algebras. Springer. (500 pages of results, but few proofs.)

3.2 Textbooks on C^* - and von Neumann algebras

- J. Dixmier: C^* -algebras. (Still very useful, in particular on applications to representation theory.)
- J. Dixmier: Von Neumann algebras. (Quite outdated, since no modular theory.)
- S. Sakai: C^* -algebras and W^* -algebras. Springer. (Rather brief.)
- R. V. Kadison and J. R. Ringrose: Fundamentals of the theory of operator algebras. Vols. 1 & 2. (Thorough, but rather slow pace.)
- G.J. Murphy: C^* -Algebras and operator theory. Academic Press. (Very accessible and readable.)
- G. Pedersen: C^* -algebras and their automorphism groups. (Good, but little on vN algebras.)
- M. Takesaki: Theory of operator algebra, vol. 1. (Very authoritative, but proofs could be more transparent.)
- M. Takesaki: Theory of operator algebra, vol. 2. (Mostly modular theory and applications)
- M. Takesaki: Theory of operator algebra, vol. 3. (Nuclear C^* -algs, hyperfinite vNAs, classification results.)
- S. Stratila and L. Zsidó: Lectures on von Neumann algebras. Abacus press 1979. (Very useful introduction to vNAs, bypassing the C^* -algs. Out of print and almost impossible to find.)
- S. Stratila: Modular theory. Abacus press, 1981. Out of print. (Takesaki's vol. 2 is preferable.)
- K. Davidson: C^* -algebras by example. AMS. (Useful example-based approach.)

3.3 K-and KK-Theory. E-theory

- Wegge-Olsen
- B. Blackadar
- M. Rordam et al: An introduction to K-theory for C^* -algebras. CUP.
- N. Higson and Roe: Analytic K -Homology. OUP.
- K.K. Jensen and K. Thomsen: Elements of KK -theory.

3.4 Noncommutative geometry

- A. Connes: Noncommutative Geometry.
- Gracia-Bondia, J.C. Varilly and H. Figueroa: Elements of noncommutative geometry. Birkhäuser.
- Khalkali and M. Marcolli (eds.): An invitation to NCG
- A. Connes and M. Marcolli: Noncommutative geometry, quantum fields and motives. AMS
- J.C. Varilly: An introduction to NCG. EMS
- N. Higson, J. Roe (eds.): Surveys in noncommutative geometry. AMS

3.5 Subfactors

- V.F.R. Jones: Subfactors and knots. AMS
- V.F.R. Jones and Sunder:
- D.E. Evans and Y. Kawahigashi: Quantum symmetries on operator algebras. OUP.