

Opgave 1 Given a function $f : \mathbb{R} \rightarrow \mathbb{R}$, define $f_t(x) = f(x - t)$, where $t \in \mathbb{R}$ is a parameter. Show that

- (a) one has pointwise convergence $\lim_{t \rightarrow 0} f_t \rightarrow f$ if and only if $f : \mathbb{R} \rightarrow \mathbb{R}$ is continuous.
- (b) one has uniform convergence $\lim_{t \rightarrow 0} f_t \rightarrow f$ if and only if $f : \mathbb{R} \rightarrow \mathbb{R}$ is uniformly continuous.